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Reg. No. :

Name :

Third Semester B.Tech. Degree Examination, April 2015 (2013 Scheme)

13.301 : ENGINEERING MATHEMATICS - II
(ABCEFHMNPRSTU)

Time: 3 Hours

Max. Marks: 100

- Instructions: 1) Answer all questions from Part A. Each question carries 4 marks.
 - 2) Answer one full question from each Module of Part B. Each full question carries 20 marks.

PART-A

- 1. Find the angle between the normals to the surface $xy = z^2$ at the points (-2, -2, 2) and (1, 9, -3).
- 2. Find the workdone by the force $\vec{F} = x\hat{i} + 2y\hat{j}$ in moving a particle from (0, 0) to (2, 2) along the curve $2y = x^2$.
- 3. Find the Fourier cosine transform of e^{-5x}.
- 4. Form the partial differential equation by eliminating the arbitrary functions from

$$z = f(y + 3x) + g(y - 3x) + \frac{x^3y}{6}$$
.

5. Solve the equation $U(x, t) = e^{-t} \cos x$ with U(x, 0) = 0 and $\frac{\partial u}{\partial t}(0, t) = 0$ by the method of separation of variables.

PART-B

Module - I

- 6. a) Show that $\vec{F} = (z^2 + 2x + 3y)\hat{i} + (3x + 2y + z)\hat{j} + (y + 2xz)\hat{k}$ is irrotational but not solenoidal.
 - b) If $\overline{r} = x\hat{i} + y\hat{j} + z\hat{k}$ and $r = |\overline{r}|$ show that $\nabla^2 r^n = n(n+1) r^{n-2}$.
 - c) Use Divergence theorem to evaluate $\iint_S \vec{F} \cdot \hat{n} \, ds$ where $\vec{F} = 4xz\hat{i} y^2\hat{j} + yz\hat{k}$ and S is the surface of the cube bounded by x = 0, x = 1, y = 0, y = 1, z = 0, z = 1.
- 7. a) Find the constants a, b, c so that $\overline{F} = (axy + bz^3)\hat{i} + (3x^2 cz)\hat{j} + (3xz^2 y)\hat{k}$ is irrotational.
 - b) If $\overline{F} = (x^2 + y^2)\hat{i} 2xy\hat{j}$. Find $\int \overline{F} \cdot d\overline{r}$ where C is the rectangle in the xy plane bounded by x = 0, x = a, y = 0, y = b.
 - c) Use Green's theorem in the plane to evaluate $\int_C (x^2 2xy) dx + (x^2y + 3) dy$ where C is the boundary of the region bounded by $y = x^2$ and y = x.

Module - II



8. a) Find the Fourier series of period 21 for the function

$$f(x) = l - x, 0 \le x \le l$$
$$= 0, \qquad l \le X \le 2 \quad l$$

- b) Expand $f(x) = \pi x x^2$ as a half range sine series in the range $(0, \pi)$.
- c) Find the Fourier transform of f(x) = x, |x| < a

$$= 0, |x| > a, a > 0.$$

- 9. a) Find the Fourier series of $f(x) = x 2x^2, -\pi < x < \pi$.
 - b) Expand $f(x) = x + \pi$, $0 \le x \le \pi$

 $= -x + \pi - \pi \le x \le 0$, given that f(x) is periodic with period 2π .

c) Find the Fourier transform of
$$f(x) = \begin{cases} 1 - x^2 & \text{if } |x| < 1 \\ 0 & \text{if } |x| > 1 \end{cases}$$

Module - III

- 10. a) Solve $\frac{\partial^2 z}{\partial x^2} + a^2 z = 0$, given that when x = 0, $z = e^y$ and $\frac{\partial z}{\partial x} = a$.
 - b) Find the singular integral of $z = px + qy + p^2 q^2$.
 - c) Solve: $x(y^2 + z) p y(x^2 + z) q = z(x^2 y^2)$.
- 11. a) Solve the equation $(D^4 D'^4)$ $z = e^{x+y}$.
 - b) Solve: $z = xp^2 + qy$.
 - c) Solve: yp = 2xy + log q.

Module - IV

- 12. a) Find the variable separable solution of the heat equation $\frac{\partial u}{\partial t} = \alpha^2 \frac{\partial^2 u}{\partial x^2}$.
 - b) If a string of length 'l' is initially at rest in the equilibrium position and each of its points is given the velocity $\left(\frac{\partial y}{\partial t}\right)_{t=0} = V_0 \cdot \sin^3 \frac{\pi x}{l}$, 0 < x < l. Find the displacement y(r, t).
- 13. a) A tightly stretched string of length 'l' is fastened at both ends. Motion is started by displacing the string into the form kx (l x) from which it is released at time t = 0. Find the displacement y (x, t).
 - b) A rod of length 'l' has its ends A and B kept at 0°C and 80°C respectively until slate-state conditions prevail. If B is suddenly reduced to 0°C and kept so, while that of A is maintained, find the temperature function u(x, t).